

Variational Principles and Mode Coupling in Periodic Structures

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Variational techniques are used in analyzing periodic "cold" microwave structures for the angular frequency, ω , as a function of assumed phase shift per periodic cell. Two variational expressions are given: one for ω in terms of the E- and H-fields, and one for $k^2 = \omega^2 \mu \epsilon$ in terms of the E-field. For structures with relatively light coupling between cells, the trial fields to be used with the variational expressions are composed of closed cavity modes, phase shifted by ϕ radians from cell to cell. Both variational expressions yield determinantal equations for $k^2(\phi)$ which agree with equations previously derived from a mode coupling point of view. One form of an equivalent lumped circuit is given to represent the structure within one of its pass bands. Curves compare the variational-mode coupling expression for $k^2(\phi)$ of a periodically lumped loaded transmission line with exact expressions.

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